Jan von Plato

Saved from the Cellar

Gerhard Gentzen's Shorthand Notes on Logic and Foundations of Mathematics

Springer

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