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**David Hilbert's Lectures
on the Foundations
of Arithmetic and Logic
1917–1933**

in collaboration with
Ulrich Majer and Dirk Schlimm

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