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Editors

Reflections on the Foundations of Mathematics

Univalent Foundations, Set Theory and
General Thoughts

 Springer

Contents

Part I Current Challenges for the Set-Theoretic Foundations	
1 Interview With a Set Theorist	3
Mirna Džamonja and Deborah Kant	
2 How to Choose New Axioms for Set Theory?	27
Laura Fontanella	
3 Maddy On The Multiverse	43
Claudio Ternullo	
Reply to Ternullo on the Multiverse	69
Penelope Maddy	
4 Proving Theorems from Reflection	79
Philip D. Welch	
Part II What Are Homotopy Type Theory and the Univalent Foundations?	
5 Naïve Type Theory	101
Thorsten Altenkirch	
6 Univalent Foundations and the Equivalence Principle	137
Benedikt Ahrens and Paige Randall North	
7 Higher Structures in Homotopy Type Theory	151
Ulrik Buchholtz	
8 Univalent Foundations and the UniMath Library	173
Anthony Bordg	
9 Models of HoTT and the Constructive View of Theories	191
Andrei Rodin	

Part III Comparing Set Theory, Category Theory, and Type Theory	
10 Set Theory and Structures	223
Neil Barton and Sy-David Friedman	
11 A New Foundational Crisis in Mathematics, Is It Really Happening?	255
Mirna Džamonja	
12 A Comparison of Type Theory with Set Theory	271
Ansten Klev	
13 What Do We Want a Foundation to Do?	293
Penelope Maddy	
Part IV Philosophical Thoughts on the Foundations of Mathematics	
14 Formal and Natural Proof: A Phenomenological Approach	315
Merlin Carl	
15 Varieties of Pluralism and Objectivity in Mathematics	345
Michèle Friend	
16 From the Foundations of Mathematics to Mathematical Pluralism ..	363
Graham Priest	
17 Does Mathematics Need Foundations?	381
Roy Wagner	
Part V Foundations in Mathematical Practice	
18 Foundations for the Working Mathematician, and for Their Computer	399
Nathan Bowler	
19 How to Frame a Mathematician	417
Bernhard Fisseni, Deniz Sarikaya, Martin Schmitt, and Bernhard Schröder	
20 Formalising Mathematics in Simple Type Theory	437
Lawrence C. Paulson	
21 Dynamics in Foundations: What Does It Mean in the Practice of Mathematics?	455
Giovanni Sambin	