

Thomas Sonar

The History of the Priority Dispute between Newton and Leibniz

Mathematics in History and Culture

With an Epilogue by Eberhard Knobloch

 Birkhäuser

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