

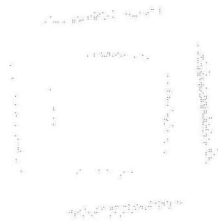
THE **ORIGIN** OF THE  
**LOGIC** OF **SYMBOLIC**  
**MATHEMATICS**

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EDMUND HUSSERL AND JACOB KLEIN

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